On Controlling Genuine Reject Rate in Multi-stage Biometric Verification

Md S. Hossain
Louisiana Tech University
Ruston, LA 71270
msh040@latech.edu

Kiran S. Balagani
New York Institute of Technology
Old Westbury, NY 11568
kbalagan@nyit.edu

Vir V. Phoha
Louisiana Tech University
Ruston, LA 71270
phoha@latech.edu

Abstract

An important problem in multi-stage biometric verification is to select an appropriate reject region. A reject region says which samples to be rejected. Rejecting impostor samples does not incur any cost in terms of user inconvenience, however, erroneously rejecting genuine samples leads to both user and administrator inconvenience. The problem becomes severe in the applications that involve a huge number of biometric transactions. Such applications necessitate the reject rate of genuine samples to be controlled. However, to date, no work has studied on controlling genuine reject rate (GRR) in multi-stage biometric verification. In this paper, we focused on controlling GRR and to this end, developed a rejection method called symmetric rejection method.

Our rejection method adds the following benefits to multi-stage biometric verification: (1) it enables the system administrator to control GRR, (2) it allows to calculate the reject region without estimation of score distributions, and (3) it does not use any assumption on the functional form of score distributions. We performed experiments on (1) two fingerprint datasets of 6000 users and (2) two face datasets of 3000 users. For fingerprint data, we achieved 18.96 percent to 70.89 percent reduction in EER by rejecting 1.5 percent to 9.4 percent genuine scores and for face data, we achieved 3.27 percent to 85.83 percent reduction in EER by rejecting 0.3 percent to 14.4 percent genuine scores.

1. Introduction

In an $n$-stage biometric verification system (e.g., [11], [10], [2], [3], [16], and [12]), if the verifier in stage $i$ is not confident enough to decide whether the sample is genuine or impostor, the sample is rejected and a new sample is submitted to the verifier in stage $i + 1$ to get a more confident decision. If all the verifiers in stages 1 through $n - 1$ fail to give a genuine or impostor decision, the verifier in stage $n$ (last stage) gives the final decision. The option to reject the ‘confusing’ samples by the verifiers in stages 1 through $n - 1$ is called reject option (see [5], [7], [17], [15], and [4]), which builds the skeleton of a multi-stage biometric verification system.

Reject option is exercised by selecting a reject region that says which samples to be rejected. Typically, a reject region consists of two reject thresholds $A$ and $C$ such that $A < C$. The sample is rejected if the corresponding score (in studies [11] and [10]) or corresponding probability ratio (in studies [3], [16], and [12]) falls inside the reject region $AC$. Based on the location and width of the reject region, different reject regions can reject different number of scores and yield different error rates. This phenomenon poses the challenge–how to select an appropriate reject region?

A reject region rejects both genuine and impostor scores. Rejecting impostor scores incurs no cost in terms of user inconvenience. However, erroneously rejecting genuine scores leads to both user and administrator inconvenience. The problem becomes severe in the applications that involve a huge number of users or biometric transactions. In such applications, selecting an inappropriate reject region (that yields huge genuine score rejection) can render the verifier impractical. Therefore, it is necessary to control the reject rate of genuine scores in each stage of multi-stage biometric verification.

However, to the best of our knowledge, no work has studied on controlling genuine (score) reject rate in multi-stage biometric verification. Rejection methods proposed in [11], [10], and [2] use the whole confusion region as the reject region. Using the whole confusion region as the reject region has two major drawbacks: 1) it rejects a large number of genuine scores, which causes severe user and administrator inconvenience and 2) by rejecting all scores inside the confusion region, it treats every score inside the confusion region in the same manner, however, the probability of a score being genuine or impostor is not same in every part of the confusion region. Rejection methods proposed in [3] and [16] calculate the reject region based on sequential probability ratio test (see [18]) and rejection method in [12] calculates the reject region based on minimum log-likelihood.
ratio. Rejection methods in [3], [16], and [12] have the following two drawbacks: 1) they assume that biometric samples are independent, which may not be true in practice (see [13] and [6]) and 2) they calculate reject region by estimating score distributions, which is an expensive and difficult task (see [8] and [14]).

In this paper, we focused on controlling the genuine reject rate (GRR) in multi-stage biometric verification. To this end, we developed a rejection method, referred to as “Symmetric Rejection Method”, to determine the reject region. Symmetric rejection method enables the system administrator to 1) control the genuine reject rate at each stage and 2) determine the reject region without estimation of genuine and impostor score densities.

We evaluated the performance of symmetric rejection method by experimenting on two biometric modalities: fingerprint and face, where each modality contains two different training sets and testing sets. In experiments, symmetric rejection method shows significant promise in reducing error rates.

Rest of the paper is organized as follows. In Section 2, we describe the proposed symmetric rejection method. In Section 3, we describe experiments and corresponding results. Finally, we conclude in Section 4 giving our future research direction.

2. Symmetric Rejection Method

Let $X$ be the genuine score set and $Y$ be the impostor score set generated by the verifier $V$ for user $U$. Let $f_G(x)$ and $f_I(y)$ be the distributions estimated from scores in $X$ and $Y$ respectively. Without loss of generality, we assume that 1) verifier $V$ outputs dissimilarity scores (and hence genuine scores are typically expected to have smaller values than impostor scores) and 2) the scores lie in the interval $[0, 1]$. Fig. 1 illustrates $f_G(x)$ and $f_I(y)$ on the scoreline $[0, 1]$. In the scoreline, $ZE_2$ is the genuine score region, $E_1O$ is the impostor score region, $E_1E_2$ is the confusion region where $f_G(x)$ and $f_I(y)$ overlap, and $B$ is the threshold where EER occurs before exercising reject option.

Below, we introduce some notation to describe the symmetric rejection method. Let $PQ$ be a region in the scoreline. Then

- $N_{G,PQ}$ is the number of genuine scores in $PQ$.
- $N_{I,PQ}$ is the number of impostor scores in $PQ$.
- $N_{G,Total}$ is the total number of genuine scores.
- $N_{I,Total}$ is the total number of impostor scores.
- $P_{G,PQ}$ is the proportion of genuine scores in $PQ$, calculated by $\frac{N_{G,PQ}}{N_{G,Total}}$.
- $P_{I,PQ}$ is the proportion of impostor scores in $PQ$, calculated by $\frac{N_{I,PQ}}{N_{I,Total}}$.

**Symmetric rejection method:** Select a reject region $AC$ (see Fig. 1) in the scoreline $[0, 1]$ such that-

$$P_{G,BC} = P_{I,AB} \quad (1)$$

where $A \in [E_1, B]$ and $C \in (B, E_2]$. That is, the proportion of genuine scores in $BC$ is equal to the proportion of impostor scores in $AB$. $AC$ is called the symmetric reject region. Here $B$ is the threshold where EER occurs before exercising reject option and $E_1E_2$ is the confusion region.

Below, we introduce some symbols corresponding to symmetric rejection:

$$\begin{align*}
\alpha_G &= P_{G,BC} & \beta_G &= P_{G,AB} & \lambda_G &= P_{G,EB_2} \\
\alpha_I &= P_{I,AB} & \beta_I &= P_{I,BC} & \lambda_I &= P_{I,E_1B}
\end{align*}$$

Then, the probability of a genuine score being rejected, genuine reject rate (GRR) can be computed as follows:

$$GRR = P_{G,AC} = \alpha_G + \beta_G. \quad (2)$$

Note that GRR is a function of $\alpha_G$. When the value of $\alpha_G$ is zero, $\beta_G$ is also zero. Therefore, no scores are rejected and GRR is zero (which is minimum). When the value of $\alpha_G$ is equal to $\lambda_G$, $\beta_G$ is equal to $P_{G,E_1B}$. Therefore, all scores inside the confusion region are rejected and GRR is equal to $\lambda_G + P_{G,E_1B}$ (which is maximum). Hence we can control GRR by setting the value of $\alpha_G$. Algorithm 1 shows how to calculate symmetric rejection region $AC$ for a given $\alpha_G$ that gives GRR equal to $\alpha_G + \beta_G$.

In Algorithm 1, note that symmetric reject region $AC$ is calculated directly from genuine and impostor scores (see steps 14-15), without estimating score densities.

**Note**-In algorithm 1, we use a function $funcOriginalEER(G, I)$ which calculates the EER before exercising reject option given array of genuine scores $G$ and array of impostor scores $I$. Because the calculation of EER before exercising reject option is trivial, we did not give details of this function.
We evaluated the performance of symmetric rejection method on a public database, namely, NIST-BSSR1 [1], [9]. NIST-BSSR1 database consists of three datasets- 1) NIST-Fingerprint-Face, 2) NIST-Fingerprint, and 3) NIST-Face. We experimented on NIST-Fingerprint and NIST-Face datasets. NIST-Fingerprint is comprised of fingerprint scores from one system run on images of 6000 individuals. For each individual, the set contains one score from the comparison of two left index fingerprints and another from two right index fingerprints. NIST-Face is comprised of scores from two face systems (C and G) run on images from 3000 individuals. For each individual, the set contains one score from the comparison of face X with a later face, Y, and a score from face X and another later face, Z. The two datasets used in our study are summarized in Table 1.

We did experiment separately for left index fingerprints, right index fingerprints, face scores from matcher C, and face scores from matcher G. Recall, we assume that the verier or matcher outputs dissimilarity scores which lie in the interval [0, 1]. However, the scores in NIST-Fingerprint and NIST-Face datasets are similarity scores and lie in different interval. Hence, to keep consistency in the experiments, we converted the similarity scores into dissimilarity scores and normalized the scores so that they lie in the interval [0, 1]. We used min-max normalization in our experiments.

For each experiment, scores from the first half users were used in training and scores from the rest half users were used in testing. We experimented with 20 different symmetric regions (ACs), obtained from the training set of genuine and impostor scores. We applied each symmetric reject region AC on the testing set and calculated corresponding equal error rates (EERs) and genuine reject rates (GRRs).

How we selected 20 ACs: We selected 20 different symmetric regions (ACs) by varying the value of α_G from zero to λ_G. Recall that when the value of α_G is zero, no scores are rejected, which is the minimum rejection, and when the value of α_G is equal to λ_G, all scores in the confusion region are rejected, which is the maximum rejection. We set the initial value of α_G to zero. Then we increment the value α_G 20 times, each time by \( \frac{\lambda_G}{20} \).

Performance metrics: We evaluated the symmetric rejection method using EER versus GRR trade-off curves that plot GRRs on the x-axis and corresponding EERs on the y-axis. Moreover, we plotted percentage reduction in EER versus GRR curves to show the performance improvement in terms of reduction in equal error rate.

For comparative study, besides applying each symmetric reject region AC on the testing set, we apply each symmetric reject region AC on the training set. We consider the EER-GRR trade-off curve obtained from the training set as the expected trade-off curve and see how much the EER-GRR curve obtained from the testing set deviate from the expected one. Low deviation indicates high promise of the symmetric rejection method in the tested biometric modality.

3.1. Results of Fingerprint Dataset

Fig. 2 and Fig. 3 show the distributions of genuine and impostor scores for left index finger and right index finger respectively. Distributions in Fig. 2a and Fig. 3a represent training sets and distributions in Fig. 2b and Fig. 3b repre-
Observation 1: The last stepsize of GRR is very high.

Observation 2: \( \lambda \) is higher than the previous step. As a consequence, in each step, the increment of GRR (except for GRR value 0.11 in right index finger dataset). For testing data of left index finger, EER decreases from 0.075 to 0.017, when GRR increases from 0 to 0.15. For testing data of right index finger, EER decreases from 0.052 to 0.0156, when GRR increases from 0 to 0.09.

Observation 3: The last stepsize of GRR is very high in all cases (for example, in case of left index finger, the last step of GRR is from 0.15 to 0.45). This is because of how we chose the symmetric reject regions (ACs). Recall, we selected 20 different (ACs), by varying the value of \( \alpha_G \), from zero to \( \lambda_G \). We incremented \( \alpha_G \) by equal step size of \( \frac{\lambda_G}{20} \). However, because the tail of the impostor score distribution is monotonically increasing, in each step, the increment of \( \beta_G \) is higher than the previous step. As a consequence, in each step, the increment of \( \text{GRR} (\alpha_G + \beta_G) \) is higher than the previous step. Therefore, in the last step the increment of GRR is very high.

Performance improvement: Fig. 5 shows that the percentage reduction in EER achieved with symmetric rejection in comparison to the EER without reject option. For left index finger, symmetric rejection achieved from 19.51 percent to 78.92 percent reduction in EER, when GRR varies from 0.0138 to 0.149 (i.e., with 1.38 percent to 14.9 percent genuine score rejection). For right index finger, symmetric rejection achieved from 18.96 percent to 70.89 percent reduction in EER, when GRR varies from 0.015 to

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### Table 1. Summary of NIST-Fingerprint and NIST-Face Datasets.

<table>
<thead>
<tr>
<th></th>
<th>NIST-Fingerprint</th>
<th>NIST-Face</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>No. of users</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Left Index</td>
<td>6000</td>
<td>3000</td>
</tr>
<tr>
<td>Right Index</td>
<td>6000</td>
<td>3000</td>
</tr>
<tr>
<td><strong>Total genuine scores</strong></td>
<td>6000*1</td>
<td>3000*2</td>
</tr>
<tr>
<td><strong>Total impostor scores</strong></td>
<td>6000*5999</td>
<td>3000*5998</td>
</tr>
</tbody>
</table>

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Figure 2. Distribution of genuine and impostor scores for left index finger. (a) Distribution for training dataset. (b) Distribution for testing dataset.

Figure 3. Distribution of genuine and impostor scores for right index finger. (a) Distribution for training dataset. (b) Distribution for testing dataset.

Figure 4. EER-GRR trade-off curve obtained by symmetric rejection method on NIST-Fingerprint dataset.

Figure 5. Percentage reduction in EER vs. GRR curve obtained by symmetric rejection method on NIST-Fingerprint dataset.
Observation 1: The last stepsize of GRR is very high.

Observation 3: EER decreases monotonically with EER-GRR trade-off curves obtained.

Fig. 9 shows that the percentage genuine score rejection is very high where the corresponding percentage genuine score rejection is very low. These results indicate that symmetric rejection is promising because percentage reduction in EER is very high where the corresponding percentage genuine score rejection is very low.

3.2. Results of Face Dataset

Fig. 6 and Fig. 7 show the distributions of genuine and impostor scores obtained by face matcher C and face matcher G. Distributions in Fig. 6a and Fig. 7a represent training sets and distributions in Fig. 6b and Fig. 7b represent testing sets. We observe that 1) for both matchers C and G, distributions of training and testing sets are almost same, which indicates that the training sets are good representatives of the testing sets, 2) proportion of genuine and impostor scores in the confusion regions for matcher C is less than that for matcher G, and 3) both genuine and impostor score distributions for matcher G are multi-modal.

Fig. 8 shows the EER-GRR trade-off curves, when symmetric rejection was applied on NIST-Face dataset. Fig. 8a shows the results for matcher C and Fig. 8b shows the results for matcher G. In each figure we plotted two curves: one curve is generated from testing score distribution and the other curve is generated from training score distribution. Our observations from Fig. 8 are listed below.

- **Observation 1:** EER-GRR trade-off curves obtained from training data and testing data are almost same for both matchers C and G. These results reflect that the training data are representatives of the testing data.
- **Observation 2:** EER decreases monotonically with the increase of GRR (except for GRR value 0.16 in matcher G dataset). For testing data obtained by matcher C, EER decreases from 0.055 to 0.007, when GRR increases from 0 to 0.144. For testing data obtained by matcher G, EER decreases from 0.067 to 0.018, when GRR increases from 0 to 0.127.
- **Observation 3:** The last stepsize of GRR is very high. The reason is same as in fingerprint.

**Performance improvement:** Fig. 9 shows that the percentage reduction in EER achieved with symmetric rejection in comparison to the EER without reject option. For matcher C, symmetric rejection achieved from 3.27 percent to 85.83 percent reduction in EER, when GRR varies from 0.003 to 0.144 (i.e., with 0.3 percent to 14.4 percent genuine score rejection). For matcher G, symmetric rejection achieved from 2.52 percent to 73.04 percent reduction in EER, when GRR varies from 0.002 to 0.127 (i.e., with 0.2 percent to 12.7 percent genuine score rejection). Similar to fingerprint, these results indicate that symmetric rejection is promising in face biometric modality.

4. Conclusion

In this paper, we developed a rejection method, called symmetric rejection method, which rejects equal proportion of genuine scores and impostor scores. Assuming dissimilarity scores, symmetric rejection method takes the EER-threshold (the threshold where equal error rate occurs before exercising reject option) as the center, and rejects a certain proportion of genuine scores from the right side of the EER-threshold, and at the same time, rejects the same proportion of impostor scores from the left side of the EER-threshold (and vice versa for similarity scores).
The symmetric rejection method advances the state-of-art as follows: 1) it enables to control the proportion of genuine scores to be rejected and 2) it enables to calculate the reject region directly from scores (see Algorithm 1, steps 14-15), without estimation of score distributions. Moreover, because symmetric rejection method does not use any assumption on the score distributions, it is applicable to all kinds of biometric modalities. As a consequence, in case of multi-modal multi-stage biometric verification systems, where different stages use different biometric modalities, symmetric rejection method appears to be more appropriate than conventional rejection methods, which depend on particular data-distributions.

We evaluated the performance of symmetric rejection method by experimenting on two biometric modalities: fingerprint and face, where fingerprint dataset contains scores from two different fingers: left index finger and right index finger and face dataset contains scores generated by two different matchers: C and G. We used a public-domain database, namely, NIST-BSSR1 [1] to create the training and testing sets. Experimental results show that for all testing sets, the symmetric rejection method performs very well in terms of EER-GRR trade-off curves. For fingerprint data, we achieved 18.96 percent to 70.89 percent reduction in EER by rejecting only 1.5 percent to 9.4 percent genuine scores. For face data, we achieved 3.27 percent to 85.83 percent reduction in EER by rejecting only 0.3 percent to 14.4 percent genuine scores.

As future work, we will study how symmetric rejection method works in other biometric modalities. Further, we will study its usability in non-biometric data, for example, how it performs in anomaly detection problem. We are also interested, in our future work, to study the optimality of symmetric rejection method.

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References


