Local Layering for Joint Motion Estimation and Occlusion Detection

Deqing Sun\textsuperscript{1} Ce Liu\textsuperscript{2} Hanspeter Pfister\textsuperscript{1}
\textsuperscript{1}Harvard University \textsuperscript{2}Microsoft Research

Figure 1. The proposed approach detects occlusions locally on a per-occurrence basis and retains uncertainty on motion and occlusion relationship during inference. It improves two baseline optical flow methods on motion estimation and has occlusion detection results comparable with a learning-based method. The pseudo depth is a visualization of the local occlusion relationship. Local layers with brighter values are likely to occlude those with darker ones. The numbers in parenthesis are the average end-point error (EPE).

Abstract

Most motion estimation algorithms (optical flow, layered models) cannot handle large amount of occlusion in textureless regions, as motion is often initialized with no occlusion assumption despite that occlusion may be included in the final objective. To handle such situations, we propose a local layering model where motion and occlusion relationships are inferred jointly. In particular, the uncertainties of occlusion relationships are retained so that motion is inferred by considering all the possibilities of local occlusion relationships. In addition, the local layering model handles articulated objects with self-occlusion. We demonstrate that the local layering model can handle motion and occlusion well for both challenging synthetic and real sequences.

1. Introduction

Despite recent advances, reliable motion estimation remains a challenging problem especially in the presence of large amounts of occlusion and textureless regions. It is well-known that correspondence and segmentation are chicken-and-egg problems. When the local grouping is known, correspondence becomes much easier. Vice versa, when correspondence is known, grouping can be reliably inferred by grouping pixels based on their motion. Existing methods, however, tend to treat each problem separately.

Optical flow\textsuperscript{12}, for example, assigns a flow vector for each pixel and completely ignores occlusion relationships between pixels. To handle occlusion, robust functions were introduced so that pixels to be occluded in the next frame may choose the right motion although the brightness constancy assumption is violated\textsuperscript{6}.

Furthermore, the aperture problem\textsuperscript{2}, namely local matching can be ambiguous, causes optical flow to fail miserably when the scene is completely textureless and occlusions prevail, such as the “two bars” sequence\textsuperscript{26} in Figure 2. The only deterministic features such as X- and T-junctions, which are often caused by occlusions, may misguide optical flow algorithms to propagate erroneous flow vectors to the rest of the image.

Although recent advances in optical flow adopt sparse feature matching to handle large-displacement\textsuperscript{8}, large amount of occlusions can easily corrupt even the state-of-the-art optical flow algorithm\textsuperscript{9}, as shown in Figure 1.

To explicitly model the grouping of pixels and the fact that some pixels will be occluded, layered models were invented and widely studied to decompose the scene into several moving layers, each of which consists of appearances, mask and motion\textsuperscript{3, 10, 14, 25}. Occlusion reasoning becomes trivial once the layers are given: a front layer occludes those behind it in every overlapping region in the image. Given the generative model, we need to infer the
reasonable results. The occlusion detection method by Humayun et al. feature embedded optical flow methods [27] fail to produce reasonable results. The occlusion detection method by Humayun et al. [13] uses output by several optical flow methods but fail to reliably detect the occlusions. Middle row: the global layered approach [23] gets stuck at the optical flow initialization by Classic+NL. Bottom row: by using superpixels [1] that well respect the static image boundaries, our local layering method correctly recovers the occlusion and motion. Motion is encoded using the color key from [5].

![Frame 1](image1) ![Frame 2](image2) ![Segmentation](image3) ![Occlusions](image4)

Figure 2. Results on the textureless “two bars” sequence [26] by different representations. Top row: classical optical flow [22] or feature embedded optical flow methods [27] fail to produce reasonable results. Middle row: the global layered approach [23] gets stuck at the optical flow initialization by Classic+NL. Bottom row: by using superpixels [1] that well respect the static image boundaries, our local layering method correctly recovers the occlusion and motion. Motion is encoded using the color key from [5].

number of layers, the layer ownership, depth ordering, and the motion for each layer. Inferring the number of layers and the relative depth ordering among all the layers is very challenging as more layers are expected.

Although promising results have been obtained from advances in layered models [23], automatically extracting layers from a video sequence is still a challenging problem. Previous work on layers relies on either motion or color cues to initialize layer segmentation. For example, an optical flow algorithm is applied first to extract motion vectors, and then clustering is used to get layer primitives [23]. Nevertheless, the optical flow in the first step can be unreliable as we have analyzed. In addition, these global layers are limited in capturing mutual or self occlusions, and often only contain a few number of layers because the complexity explodes as the number of layers increases. Therefore, existing layered models are more suitable for characterizing scenes with several big plane motions but are fundamentally limited in capturing scenes containing articulated objects.

Some occlusion detection methods use optical flow as a feature, although the flow is estimated with the assumption of no occlusion. Humayun et al. [13] treat occlusion detection as a binary classification problem. They propose to use optical flow estimated by a number of different algorithms to generate features for the random forest classifiers. Training takes significant amount of time and errors in optical flow estimation may propagate to occlusion detection. Stein and Hebert [21] extract various mid-level features to predict occlusion boundaries. Sundberg et al. [24] compute features from optical flow and obtain significant improvement in predicting occlusion boundaries. However, all methods are separate from motion estimation and neither uses the detected occlusion (boundaries) to improve optical flow.

Ayvaci et al. [4] use a sparse prior to model occlusion and jointly solve optical flow and occlusion. Their occlusion reasoning is mainly based on the data matching error and a sparse prior, similar to the outlier process. The model has no notion of foreground and background to geometrically reason about occlusions using the motion. Black and Fleet [7] propose to locally track an individual patch over time to reason about occlusion and motion boundaries. They use the velocity on both sides of the occlusion boundaries to predict the (dis)occlusions of pixels. However, their method does not work for textureless scenes, such as the “two bars” example [26] in Figure 2. Yamaguchi et al. [28] jointly estimate the motion of superpixels and the occlusion boundaries between superpixels for epipolar-constrained optical flow estimation [11]. While the occlusion boundaries are used for locating motion boundaries, the method does not use the motion of superpixels to detect occlusion.

In this paper, we attempt to jointly infer motion and occlusion by means of a local layering model\(^1\). Our model works on superpixel representations obtained from oversegmentation. We not only model the motion for each superpixel like previous work, but also explicitly model the occlusion relationships between neighboring super-pixels. The motion of every superpixel, therefore, depends on its occlusion relationships with its neighbors. Compared with global layered models, our approach decides occlusion locally and does not require strictly ordering all the layers in depth. In the inference, we keep the uncertainties of both motion and occlusion relationships so that motion is inferred by considering all the possibilities of local occlusion relationships and vice versa, the occlusion relationship is inferred by considering all possible motion vectors. To reduce the huge solution space for the motion, our method uses the output of optical flow methods as candidates and improves the baseline methods, particularly in occlusion regions.

We have tested our model on both toy and real examples. Our local layered model solves the challenging two-bar s-
timulus. We have also evaluated our method on the MPI Sintel database [9] and demonstrated that our method improves the baseline algorithms that provide the motion candidate for our method, and also performs comparably with one learning-based occlusion detection algorithm [13].

2. Representation and Visualization

The local layering representation. Consider the scene in Figure 6(a). Even though we can have a semantic segmentation of the scene into apple and hand layers, global layers still have difficulty in modeling the mutual occlusion between the hand and the apple and self-occlusion of the hand. However, occlusion reasoning becomes feasible if we model the phenomenon locally on a per occurrence basis [18]. We propose to model the scene using a set of local layers to handle complex occlusions. Each local layer explains a small local region and has its own motion. Mutual occlusion is unlikely because of the small size of the local layers. The local layering representation only requires the segmentation boundaries to be consistent with the motion boundaries.

Given a pair of images $I_t$ and $I_{t+1}$, the unknowns include a segmentation of the first frame into local layers, the motion of each local layer, the occlusion relationship between spatially close local layers, and the occlusion map for the first frame. To simplify the problem, we pre-segment the first frame using the SLIC superpixel algorithm [1] with static image (and motion) cues. In the rest of the paper, we use local layers and superpixels exchangeably. Now we need to infer the motion $\mathbf{m}$ of every local layer, the occlusion relationship between layers $\mathbf{R}$, and a per-pixel occlusion map $\mathbf{o}$. There are three relationships between two local layers $i$ and $j$: $i$ occludes $j$ ($R_{ij} = 1$), $i$ and $j$ move together ($R_{ij} = 0$), and $j$ occludes $i$ ($R_{ij} = -1$), as shown in Figure 3. A pixel $p$ is occluded if $o_p = 1$ and visible if $o_p = 0$.

The pseudo depth visualization. To better visualize the local occlusion relationship, we derive a global pseudo depth map from the occlusion relationship, as shown in Figure 1(b). The brighter a local layer’s pseudo depth is, the more likely will this local layer occlude other ones. Let $d_i$ be the pseudo depth for the $i$th superpixel. We compute the pseudo depth to satisfy the following constraints

$$d_i - d_j = R_{ij},$$

If superpixel $i$ occludes $j$, i.e., $R_{ij} = 1$, we enforce the pseudo depth of $i$ to be larger than that of $j$. If $i$ is occluded by $j$, we enforce the pseudo depth of $i$ to be smaller than that of $j$. If $i$ and $j$ move together, we encourage their pseudo depths to be the same. We can obtain a system of linear equations for the pseudo depth

$$A \mathbf{d} = \mathbf{b},$$

where the set $\mathcal{N}_i^+$ contains all the spatially close superpixels that may bump into $i$ in the next frame, $A(i, j) = |\mathcal{N}_i^+|$, $A(i, j) = -1, j \in \mathcal{N}_i^+$ and 0 otherwise, and $b(i) = \sum_{j \in \mathcal{N}_i^+} R_{ij}$. Solving the linear equation system gives the pseudo depth (for singular $A$, we compute the pseudo inverse). Figure 4 shows the constraints and results for a toy example. The occluding local layers are assigned larger pseudo depth values than the occluded ones, while local layers moving together are assigned similar values.

3. Probabilistic Model

We adopt a probabilistic approach to model the dependence between the observed and the unknowns and their priors. Figure 5 shows our graphical model. We use an EM algorithm to maximize the posterior probability density function (p.d.f.) of the motion and the occlusion relationship, while marginalizing over the per-pixel occlusion map

$$\{\hat{\mathbf{m}}, \hat{\mathbf{R}}\} = \arg\max_{\mathbf{m}, \mathbf{R}} \sum_{\mathbf{o}} p(\mathbf{m}, \mathbf{o}, \mathbf{R}|I_t, I_{t+1}),$$

Figure 3. Three possible occlusion relationships between two local layers $i$ and $j$. The set $\Omega_{i\rightarrow j}$ contains the pixels in $i$ that bump into pixels in $j$ at the next frame and similarly for $\Omega_{j\rightarrow i}$. Note that $\Omega_{i\rightarrow j}$ and $\Omega_{j\rightarrow i}$ depend on the unknown motion.

Figure 4. A toy example to explain the computation of pseudo depth from the local occlusion relationship. The brightest top left patch occludes its two neighboring patches, while the rest three patches move together.
where the posterior factorizes as
\[
p(m, o, R|I_t, I_{t+1}) \propto p(I_{t+1}|o, m, I_t)p(o|R, m)p(R|m)p(m|I_t),
\]
where the first (data) term describes how to generate the next frame given the current frame, the motion, and the occlusions, the second and third terms encodes the constraints among motion, occlusion, and occlusion relationship, and the last one is the conditional motion prior. We will explain each term as follows.

**Data term.** The data term tells how we can generate the next frame from the current frame, the motion, and the occlusion map. Generally, if a pixel is visible, the appearance of this pixel at the current frame gives strong constraint on the appearance of the corresponding pixel at the next frame. However, an occluded pixel has no corresponding pixel at the next frame and should not be used for generating the next one. Hence
\[
-\log p(I_{t+1}|o, m, I_t) \propto \sum_i \sum_p \left[ \rho_D(I_i^t - I_{i+1}^{t+mp})\delta_p + \lambda_O o_p \right],
\]
where the set \(\Omega_t\) contains all the pixels in the \(t\)th local layer, \(\rho_D\) is a robust penalty function, \(\lambda_O\) is a constant penalty for occlusion, and \(o_p = 1 - \delta_p\). This data term has been used in previous global layered models [23] on a per-pixel basis.

To gain some intuition, we plot the sum of squared difference (SSD) surface for a superpixel with occlusions in Figure 6. The minimum of the SSD surface is far from the true motion in the presence of large occlusions. If we disable the occluded pixels, the minimum of the modified SSD surface is close to the ground truth motion. For superpixels with occluded region, the data term in Eq. (5) mainly relies on their visible pixels.

**Motion prior.** Our prior for the motion of local layers is similar to that for optical flow. Both encode the fact that motion of real-world objects is smooth and slow, but occasionally abrupt [20]. We assume that abrupt motion tends to happen at object boundaries, across which appearances often change. Our conditional motion prior is
\[
-\log p(m|I_t) \propto \sum_i \left\{ \sum_{p \in \Omega_i} \lambda_S \rho_S(m_p) + \sum_{j \in \mathcal{N}_i} \lambda_F \omega_{ij} \rho_F(m_i - m_j) \right\},
\]
where the set \(\mathcal{N}_i\) contains all the spatially neighboring local layers of \(i\), \(\bar{m}_i\) is the average motion of pixels in the local layer \(i\), and \(\omega_{ij} = \max \left\{ \exp\left(-\frac{||I_i - I_j||^2}{\sigma_i^2}\right), T \right\}\). in which \(\bar{I}_i\) is the mean color of the local layer \(i\), \(\sigma_i\) is the standard deviation of the Gaussian kernel, and \(T\) is a threshold. The weights allow motion boundaries to lie between superpixels with different appearances. Again \(\lambda_S\) is a constant and \(\rho_S\) is a robust penalty function.

**Motion and occlusions.** If motion is known, it provides constraints to the occlusion relationship, as shown in Figure 3. Specifically, if two local layers overlap each other at the next frame according to their motion, then their occlusion relationship should indicate the occurrence of occlusion; otherwise, the occlusion relationship should prefer the “moving together” explanation. The conditional distribution of the occlusion relationship given the motion encodes the constraints as
\[
-\log p(R|m) \propto \sum_i \sum_{j \in \mathcal{N}_i} \lambda_P \left\{ \delta(|\Omega_i \rightarrow j| \neq 0) \delta(R_{ij} = 0) + \delta(|\Omega_i \rightarrow j| = 0) \delta(R_{ij} \neq 0) \right\},
\]
where the first term enforces that, when two local layers bump into each other at the next frame (the \(R_{ij} = 1\) and \(R_{ij} = -1\) images in Figure 3), one layer should occlude another, while the second term enforces that, when two local layers have no overlap (the \(R_{ij} = 0\) image in Figure 3), they should move together. The indicator function \(\delta(x) = 1\) if \(x\) is true and 0 otherwise. \(\lambda_P\) is a constant penalty to penalize the “forbidden” states. The set \(\Omega_i \rightarrow j\) contains the pixels in \(i\) that overlap \(j\) at the next frame, as shown in Figure 3.
Joint motion and occlusion relationship reasoning. Given the probability of pixels being occluded, we jointly estimate the motion and the occlusion relationship by minimizing Eq. (12). The motion state space is huge even when we assume a single integer translational motion for each local layer. Hence we restrict the motion space to a few candidate motion fields for large images. Given fixed motion candidates, we run min sum algorithm on the loopy graph [15, 19] to minimize Eq. (12). We propose several schemes to generate candidate motion fields. One scheme is to pre-select several optical flow fields as candidates. Each local layer can take the motion at the corresponding position from these candidate flow fields. Another scheme is to use one optical flow field, cluster the flow vectors by kmeans to construct additional constant flow fields as candidates [16]. Finally, we also test sampling the motion space around the current solution during the inference. We then adaptively keep the top motion candidates and sample around them. When the iteration stops, we threshold the occlusion probability to decide the occlusion state of every pixel. Figure 8 shows the change of the unknowns during the iteration for the textureless “two bar” sequence in Figure 2. With more iterations, the solution by the proposed method converges to the correct occlusion and motion.

Table 1. The algorithm for the local layering algorithm. The sampling step is omitted if we use a fixed motion space.

<table>
<thead>
<tr>
<th>Input: frames $I_t$ and $I_{t+1}$</th>
</tr>
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<tbody>
<tr>
<td>Initialize: compute SLIC superpixels [1] and optical flow [22, 27]; sample integer motion around optical flow</td>
</tr>
<tr>
<td>Loop until convergence (outer iteration)</td>
</tr>
<tr>
<td>- Compute the probability of being occluded (Eq. (9))</td>
</tr>
<tr>
<td>- Solve for motion and occlusion relationship: loop until convergence (inner iteration)</td>
</tr>
<tr>
<td>- Select and sample around top motion states</td>
</tr>
<tr>
<td>- Perform loopy belief propagation (Eq. (12))</td>
</tr>
<tr>
<td>Threshold the occlusion probability</td>
</tr>
<tr>
<td>Refine motion with detected occlusion</td>
</tr>
<tr>
<td>Output: motion, occlusion relationship, and occlusions</td>
</tr>
</tbody>
</table>
Beliefs on motion for one layer

Occlusion probability

Occlusion (black)

Motion

Figure 8. Convergence of the inference algorithm on the “two bars” sequence in Figure 2. By retaining uncertainty on both motion and occlusion relationship, the proposed method converges to the correct motion and occlusion.

The motion prior for local layers may not accurately describe the interaction within each local layer. To further improve the motion, we use the estimated motion and occlusion to initialize a modified optical flow method. Specifically, we disable the data term of the “Classic+NLP” method [22] in the detected occlusion regions to refine the estimated motion by our local layering method.

5. Results

We evaluate the proposed method on both synthetic data and the MPI Sintel dataset. For motion estimation, we compare the proposed method to two widely used optical flow methods: Classic+NL-FastP [22] and MDP-flow2 [27]. For occlusion detection, we compare the proposed method to one state-of-the-art learning-based occlusion detector [13]. We use the code from the authors’ website. For [13], we added additional data from Sintel to train the “lean” version of its classifier. The code [13] outputs the probability of every pixel being occluded. We select the best threshold according to the GT occlusion to obtain the hard occlusion map.

\[
E(m, R) = \sum_i \left\{ \sum_{p \in \Omega_i} \left\{ \rho_D(I_P^t - I_{t+1}^P)(1 - \Pr(o_p = 1)) + \lambda_o \Pr(o_p = 1) + \lambda_s \rho_S(m_p) \right\} + \sum_{j \in N_i} \lambda_{\rho_F} w_{ij} \rho_F(\bar{m}_i - \bar{m}_j) \right\} + \sum_{j \in N_i^+} \left\{ \lambda_o \delta(\Omega_{i \to j} \neq 0) \delta(R_{ij} = 0) + \delta(\Omega_{i \to j} = 0) \delta(R_{ij} \neq 0) \right\} + \sum_{p \in \Omega_i} \lambda_{\rho_e} \{ Pr(o_p = 1) \delta(R_{ij} \geq 0) + (1 - \Pr(o_p = 1)) \delta(R_{ij} \leq 0) \} \right\}. 
\]

\[ (12) \]

Synthetic data. We first test on the classical “two bars” sequence [26], as shown in Figure 2. The sequence is challenging because it is textureless, has false T junctions, and contains occlusions. Weiss and Adelson [26] propose a layered method for the “two bars” sequences. Their method requires a perfect segmentation of the scene as input. Liu et al. [17] analyze the contour motion particularly for textureless sequences. The output is sparse motion for the contours and cannot be directly interpolated to be dense motion field. The MDP-Flow2 [27] method fails because the false T junctions breaks down the feature matching component of the method. The “Classic+NLP” [22] method also fails because of the textureless surfaces and the occlusions. We use a full solution space for the motion that covers the ground truth for this toy example. The proposed method correctly recovers the motion and the occlusions by locally reasoning about occlusions among over-segmented superpixels. Note that the slow motion prior is important to recover the background motion. Adding texture noise to the synthetic sequences helps the optical flow methods obtain better results, while the proposed method performs as well.

MPI Sintel. We test the proposed method using the MPI Sintel dataset [9]. These sequences contain complex occlusions that challenge the state of the art. Figure 9 shows the results on several challenging sequences by the proposed method and the baseline optical flow methods. By analyzing the occlusions locally on a per-occurrence basis, the proposed method detects most of the occlusions. The detected occlusions help recover the motion in the large occlusion regions, such as the background occluded by the hand, the leg, and the small dragon.

As summarized in Table 2, the proposed method improves the optical flow methods [22, 27] that serve as candidates, particularly in the unmatched (occlusion) regions. We further test some variants of the proposed method using a representative subset of the training clean set (the 1st, 5th, and 23rd image pairs from each of the 23 sequence). We find that adding motion cue to the SLIC algorithm results in slightly more accurate results (MotionSLIC in Table 3), suggesting benefits to jointly solve for segmentation, motion, and occlusions. We test two simple methods to construct diverse motion candidates but find no overall improvement (MDP-Kmeans3 and MDP-Sampling in Table 3).

We also evaluate the occlusion detection results in Ta-
Table 2. Average end-point error (EPE) results on the MPI Sintel test set. Unmatched correspond to the occlusion regions.

<table>
<thead>
<tr>
<th></th>
<th>Clean</th>
<th>Final</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>all</td>
<td>unmatched</td>
</tr>
<tr>
<td>CNL-fastP [22]</td>
<td>6.940</td>
<td>37.866</td>
</tr>
<tr>
<td>MDP-Flow2 [27]</td>
<td>5.837</td>
<td>38.158</td>
</tr>
<tr>
<td>Proposed</td>
<td>5.820</td>
<td>37.884</td>
</tr>
</tbody>
</table>

Table 3. Average end-point error (EPE) results by two baseline optical flow methods, the proposed method and its variants on 69 clean image pairs from the MPI Sintel training set.

<table>
<thead>
<tr>
<th></th>
<th>all</th>
<th>unmatched</th>
</tr>
</thead>
<tbody>
<tr>
<td>CNL-fastP [22]</td>
<td>5.149</td>
<td>11.155</td>
</tr>
<tr>
<td>MDP-Flow2 [27]</td>
<td>4.002</td>
<td>12.182</td>
</tr>
<tr>
<td>Proposed (CNL+MDP)</td>
<td>3.763</td>
<td>10.287</td>
</tr>
<tr>
<td>Proposed (MotionSLIC)</td>
<td>3.719</td>
<td>10.252</td>
</tr>
<tr>
<td>Proposed (MDP-Kmeans3)</td>
<td>4.492</td>
<td>11.990</td>
</tr>
<tr>
<td>Proposed (MDP-Sampling)</td>
<td>4.362</td>
<td>12.002</td>
</tr>
</tbody>
</table>

Table 4. Average F-measure (larger better) for occlusion detection, averaged over 69 MPI Sintel sequences. The oracle threshold is determined using the GT occlusion.

<table>
<thead>
<tr>
<th></th>
<th>oracle</th>
<th>fixed (0.5)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Humayun et al. [13]</td>
<td>0.535</td>
<td>0.448</td>
</tr>
<tr>
<td>Proposed</td>
<td>0.474</td>
<td>0.376</td>
</tr>
</tbody>
</table>

6. Conclusions

We have introduced the local layering representation for motion estimation and occlusion detection. This flexible representation enables us to capture complex occlusions without resorting to a fully 3D model. We find that locally deciding the depth ordering on a per-occlusion basis is feasible when we jointly infer motion and occlusion relationship and retain the uncertainty on both during inference. Our simple representation achieves promising results on both the “two bars” sequence and the MPI Sintel dataset. The detected occlusions are close to the ground truth, even for complex occlusions. Our method improves over the baseline optical flow methods particularly in occlusion regions. Our work opens new avenues to jointly modeling motion and occlusions and suggests that exploring richer and more flexible representations can be fruitful for this challenging problem.

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References

[22] D. Sun, S. Roth, and M. J. Black. A quantitative analysis of current practices in optical flow estimation and the principles behind them. *IJCV*, 106(2):15–137, 2014. 1, 2, 3, 5, 6, 7, 8
Figure 9. The proposed method produces reasonable occlusion detection results, which helps recover the motion of the region occluded by the hand in the top row, the leg in the middle row, and the dragon in the bottom row. The numbers in parenthesis are the average EPE.

Figure 10. More motion estimation and occlusion detection results. The detected occlusion boundaries by the proposed method are close to the ground truth. The brighter its pseudo depth is, the local layer is more likely to occlude other local layers.


